

Critical Role of High Permeability Zones on Field-Scale Pathogen Transport and Retention, Infection Risk, and Setback Distance

Scott A. Bradford¹, Feike J. Leij², Jack Schijven³,
and Saeed Torkzaban⁴

¹US Salinity Laboratory, USDA, ARS, Riverside, CA

²Department of Civil Engineering, California State University,
Long Beach, CA

³Faculty of Geosciences, Utrecht University, The Netherland

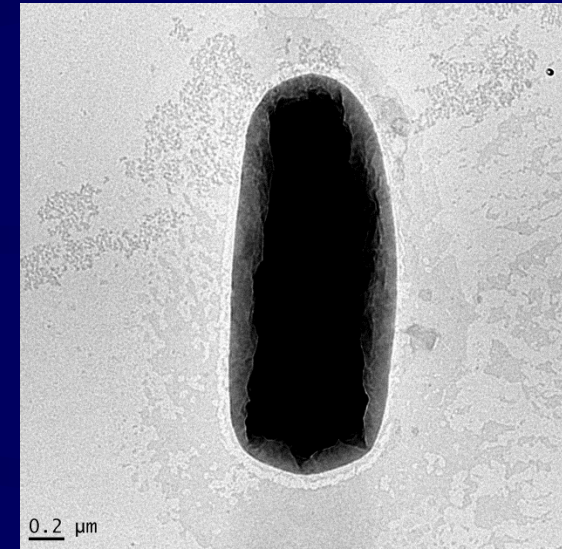
⁴CSIRO Land and Water, Glen Osmond, Australia

Funding Sources: USDA NP 212

Pathogens

- Groundwater is the principal source of drinking water for as many as 2 billion people worldwide (50% in US and 75% in Europe).
- 52% of drinking-water outbreaks are associated with groundwater in the US.
- 15% of groundwater systems in the US and Canada tested positive for enteric pathogens (bacteria, virus, and protozoan parasites).
- Waterborne illnesses have been estimated to kill 2-3 million people worldwide every year.

E. coli O157:H7



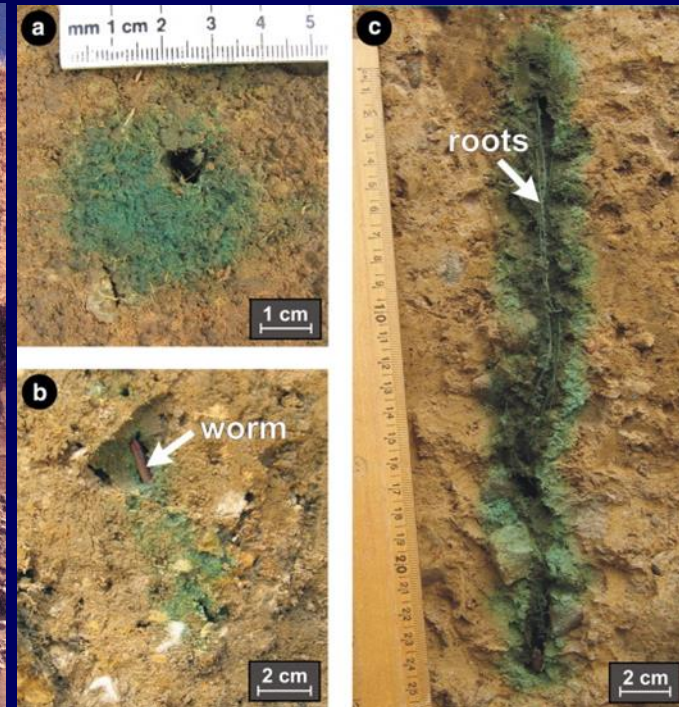
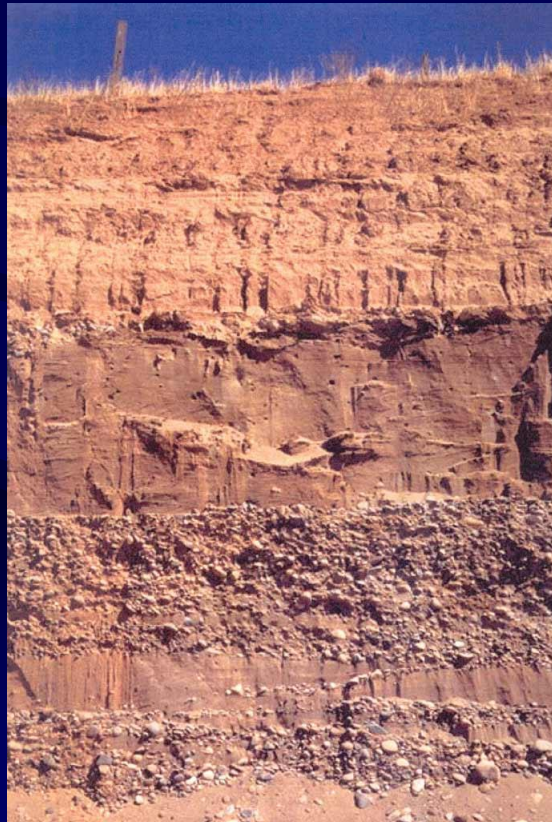
Cryptosporidium parvum

Objective

- Develop mathematical models to examine the role of high permeability zones on pathogen transport and fate.
- Examples of high permeability zones:
 - Preferential flow paths
 - Sand and gravel layers and lenses
 - Fractured rock
 - Karst systems



USGS



Cey et al. (2009)

Deterministic Pathogen Transport

- **Advective-dispersion equation with retention, release, and decay**

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2} - v_w \frac{\partial C}{\partial z} - (\mu_w + k_{sw})C + \frac{\rho_b k_{rs}}{\theta} S_r$$

$$\rho_b \frac{\partial S_r}{\partial t} = \theta F_{rev} k_{sw} C - \rho_b (\mu_s + k_{rs}) S_r$$

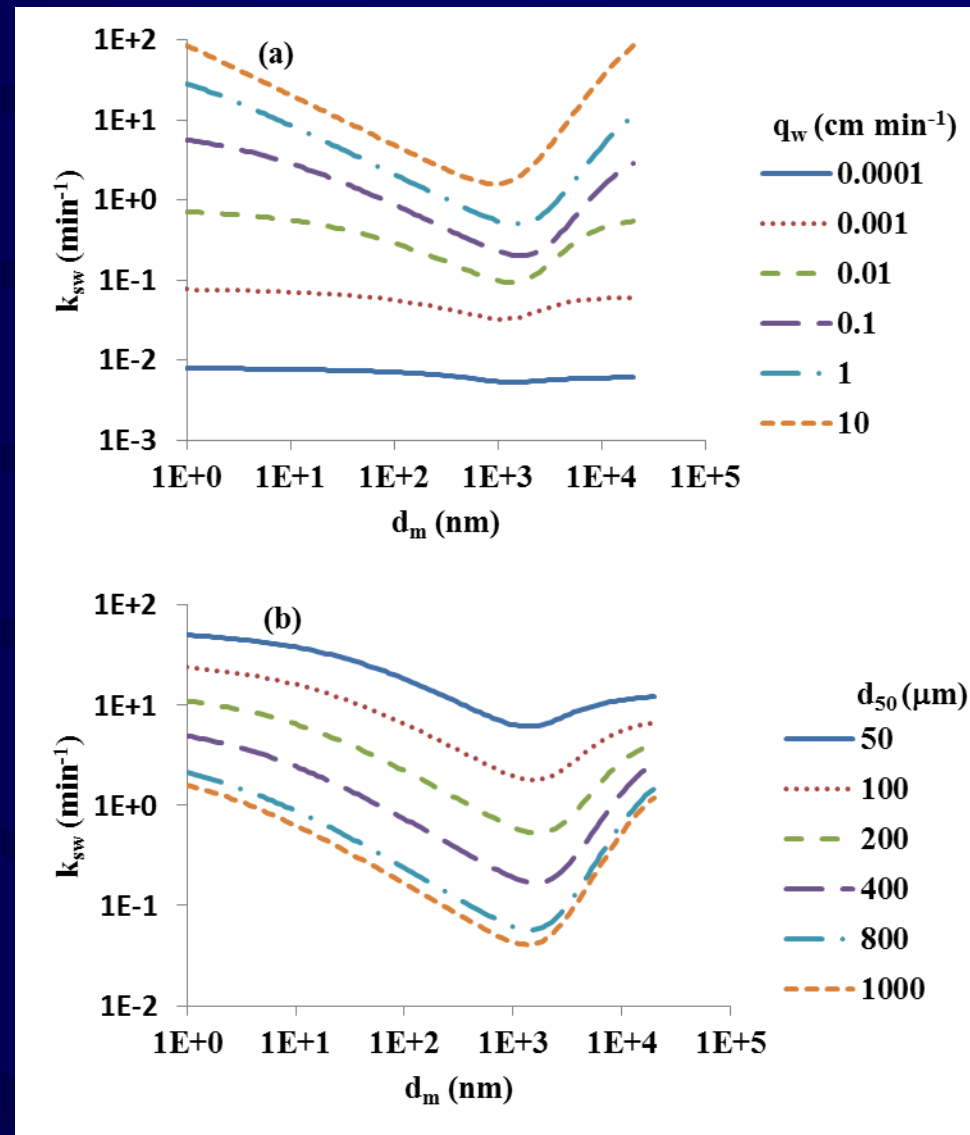
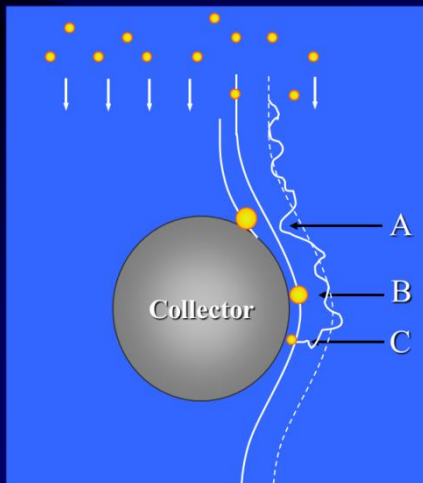
$$\rho_b \frac{\partial S_i}{\partial t} = \theta (1 - F_{rev}) k_{sw} C - \rho_b \mu_s S_i$$

- **We use an analytic solution from Toride et al. (1995)**
- **Filtration theory**

$$k_{sw} = \frac{3(1 - \theta)}{2d_{50}} \eta \alpha v_w$$

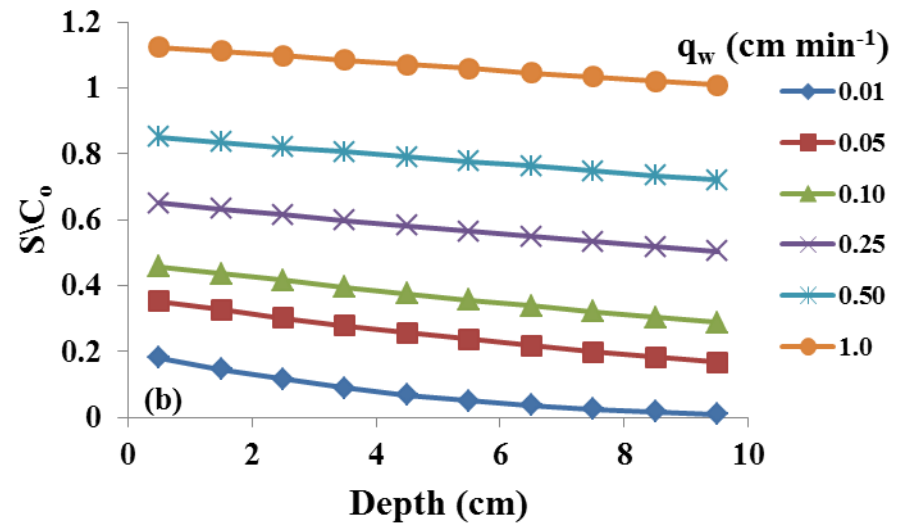
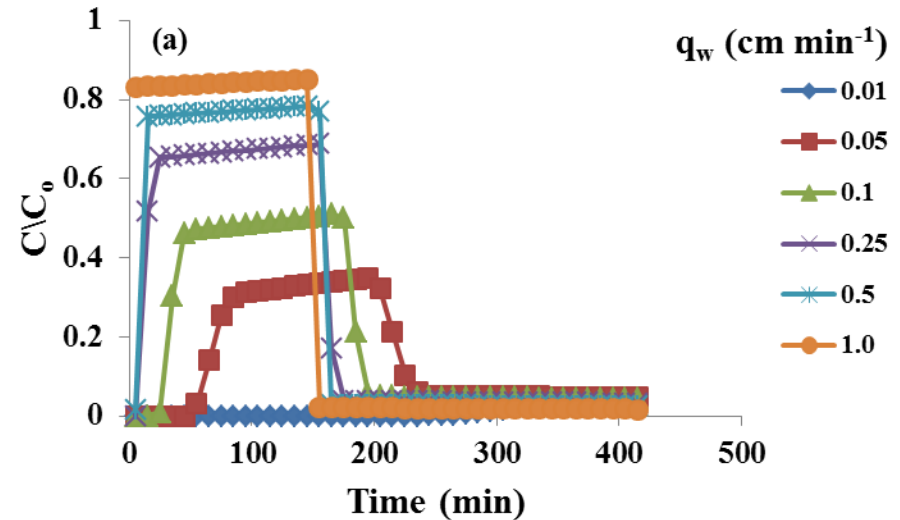
Filtration Theory

- Mass transfer occurs via sedimentation (A), and interception (B), and diffusion (C).
- Mass transfer is quantified by solution of the convective diffusion equation.



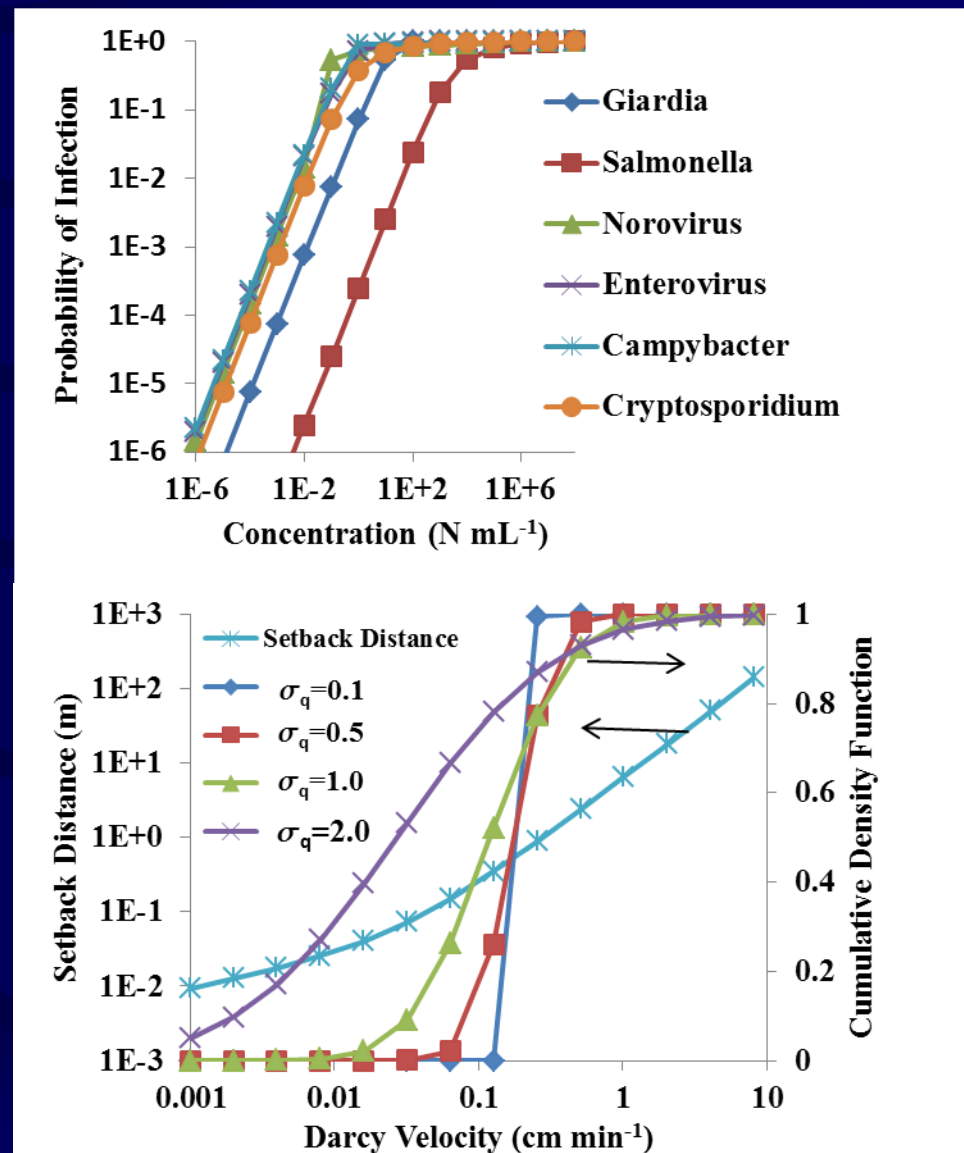
Filtration Theory Prediction

- Filtration theory predicts that k_{sw} increases with velocity.
- However, there is a decrease in residence with increasing q_w that produces less retention.
- Retention profile is exponential with transport distance.



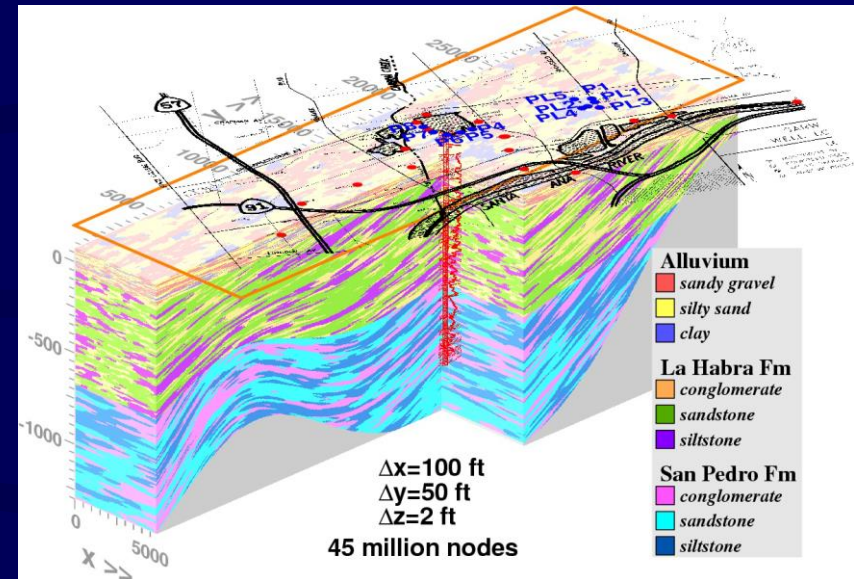
Setback Distance and Velocity

- Probability of infection depends on the amount of water consumed, the concentration of pathogens, and dose-response model.
- Transport (setback) distance is needed to remove pathogens (> 6 logs) from source water.
- Setback distance increases with velocity.
- High velocity regions will control the risk of infection.



Deterministic Models

- Deterministically model subsurface heterogeneity in flow and transport properties.
- Does not account for uncertainty.
- Alternative deterministic models
 - Dual permeability models
 - Analytic solution from Leij and Bradford (2013)



Maxwell et al. (2003)

$$\theta_1 \frac{\partial C_1}{\partial t} = \theta_1 D_1 \frac{\partial^2 C_1}{\partial z^2} - \theta_1 v_1 \frac{\partial C_1}{\partial z} - \theta_1 (\mu_w + k_{sw1}) C_1 + \rho_b k_{rs1} S_{r1} - \theta_1 \Gamma (C_1 - C_2)$$

$$\theta_2 \frac{\partial C_2}{\partial t} = \theta_2 D_2 \frac{\partial^2 C_2}{\partial z^2} - \theta_2 v_2 \frac{\partial C_2}{\partial z} - \theta_2 (\mu_w + k_{sw2}) C_2 + \rho_b k_{rs2} S_{r2} + \theta_1 \Gamma (C_1 - C_2)$$

$$\rho_b \frac{\partial S_{r1}}{\partial t} = \theta_1 F_{rev} k_{sw1} C_1 - \rho_b (\mu_s + k_{rs1}) S_{r1}$$

$$\rho_b \frac{\partial S_{i1}}{\partial t} = \theta_1 (1 - F_{rev}) k_{sw1} C_1 - \rho_b \mu_s S_{i1}$$

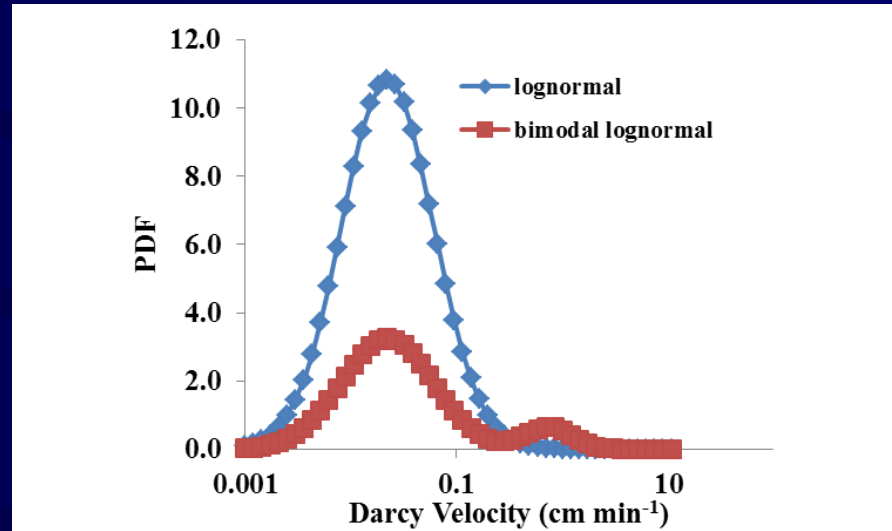
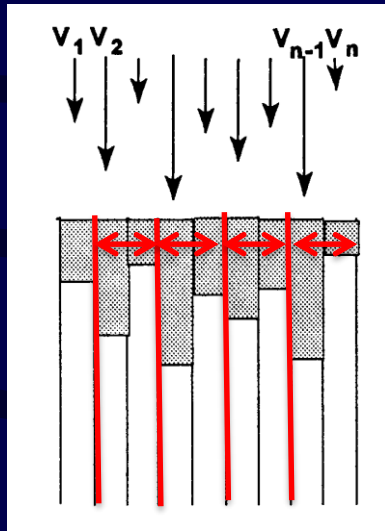
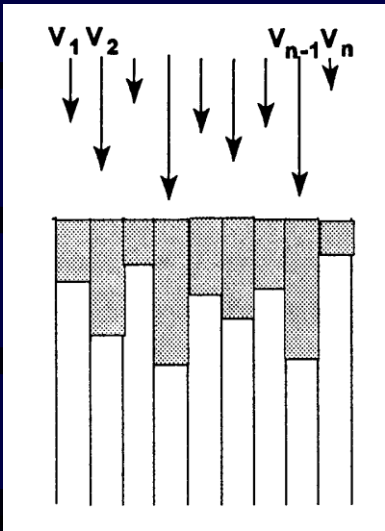
$$\rho_b \frac{\partial S_{r2}}{\partial t} = \theta_2 F_{rev} k_{sw2} C_2 - \rho_b (\mu_s + k_{rs2}) S_{r2}$$

$$\rho_b \frac{\partial S_{i2}}{\partial t} = \theta_2 (1 - F_{rev}) k_{sw2} C_2 - \rho_b \mu_s S_{i2}$$

Wang et al. (2014)

Stochastic Stream Tube Model (SSTM)

- Field-scale flow and transport are described using a series of independent stream tubes.
- Local-scale transport is described deterministically using single or dual permeability models.
- Field-scale parameters are described with PDFs.



- More complex geometries (variable width and tortuous) may be considered.
- Mean and variance of field-scale concentrations can be calculated.

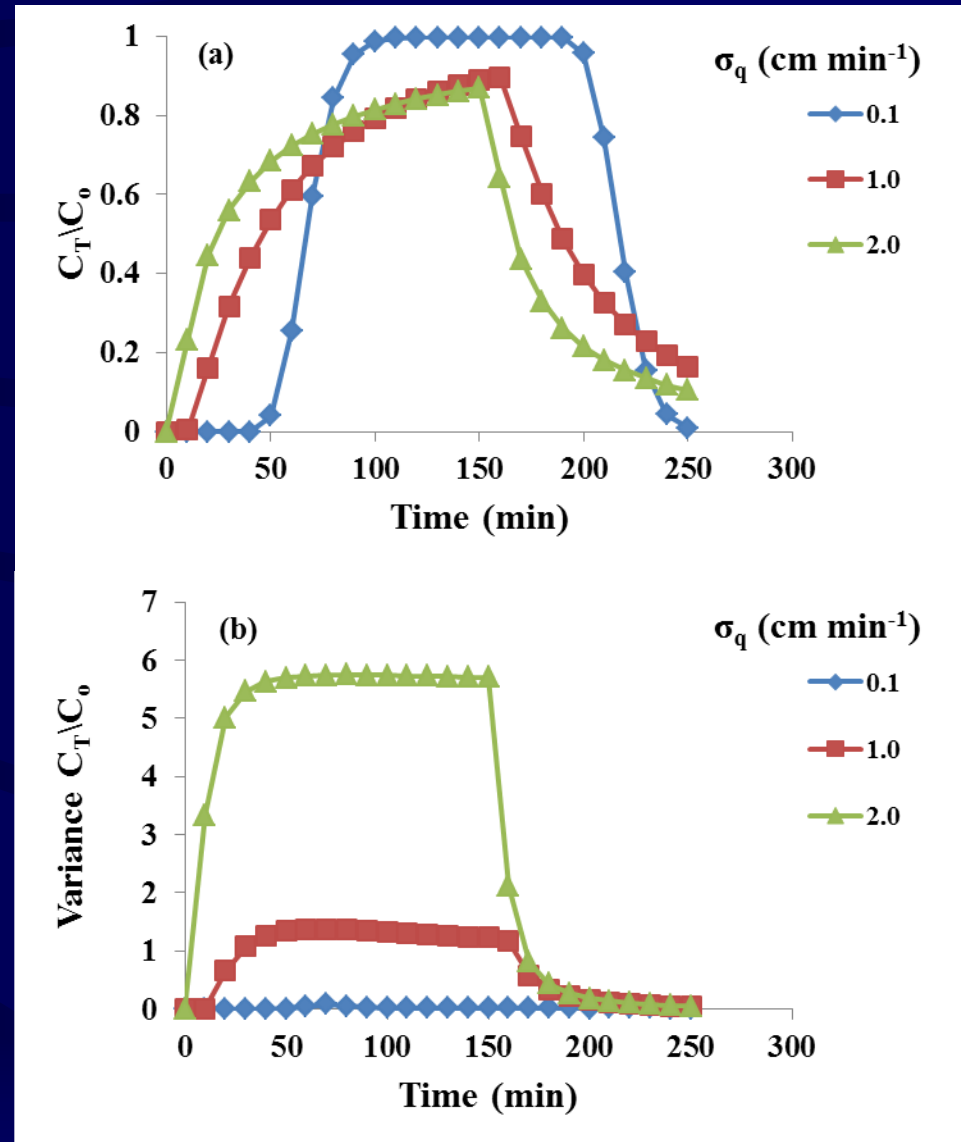
$$C_T(z, t) = \frac{\langle q_w C(z, t; q_w) \rangle}{\langle q_w \rangle} = \frac{\int_0^{\infty} q_w f(q_w) C(z, t; q_w) dq_w}{\int_0^{\infty} q_w f(q_w) dq_w}$$

$$C_T(z, t) = \frac{\langle q_1 C_1(z, t; q_w) + q_2 C_2(z, t; q_w) \rangle}{\langle q_w \rangle} = \frac{\int_0^{\infty} f(q_w) [q_1 C_1(z, t; q_w) + q_2 C_2(z, t; q_w)] dq_w}{\int_0^{\infty} q_w f(q_w) dq_w}$$

- Dual permeability stream tube model allows for mixing!

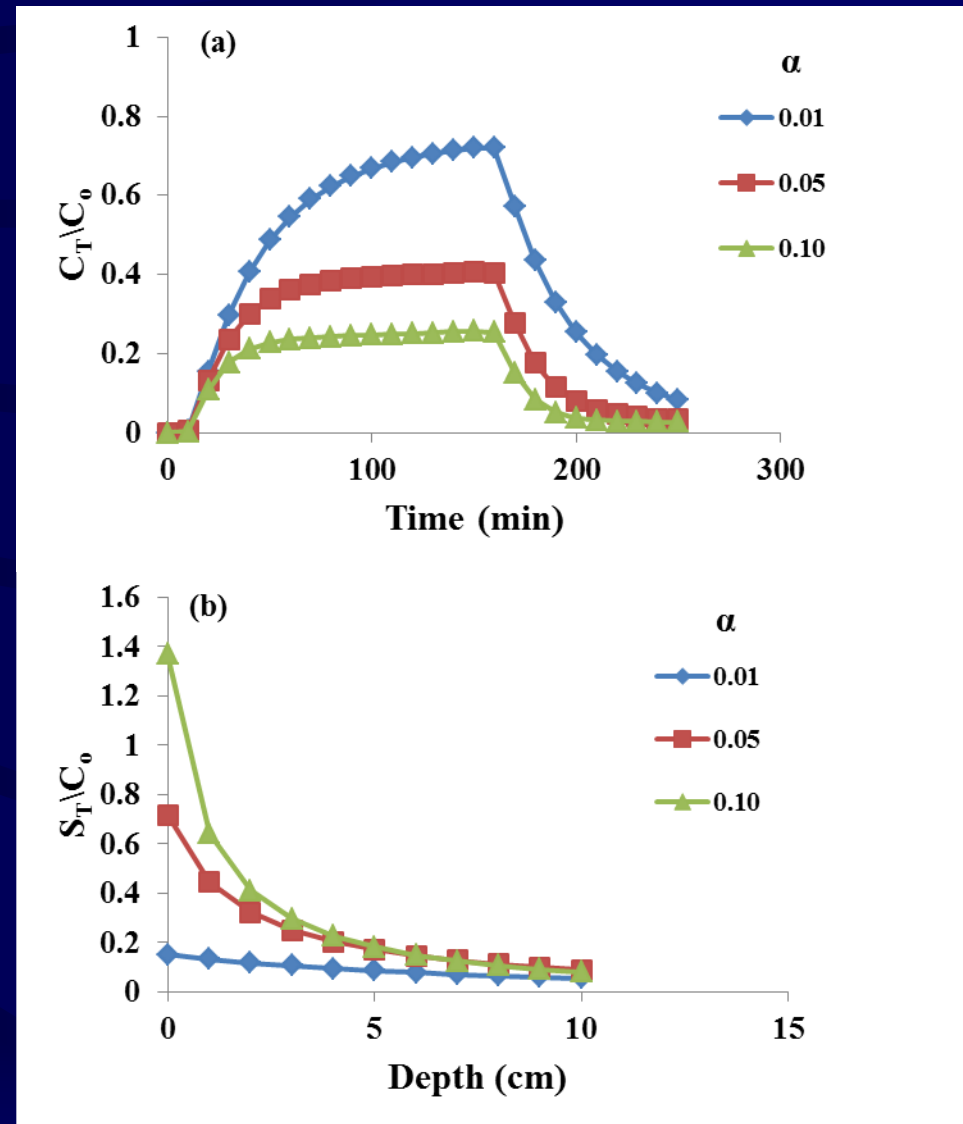
SSTM – Single Permeability Per Tube

- Ex. – Conservative tracer
- Earlier breakthrough and concentration variance with increasing velocity variance.
- Tailing is due to physical non-equilibrium.



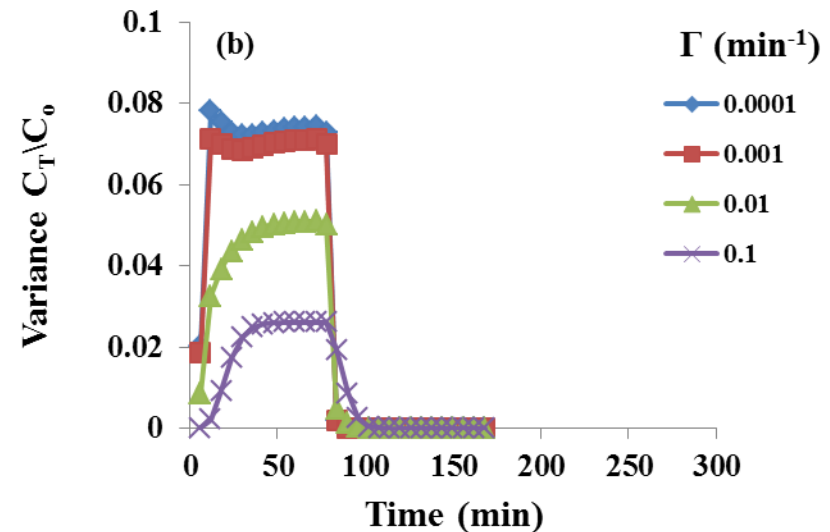
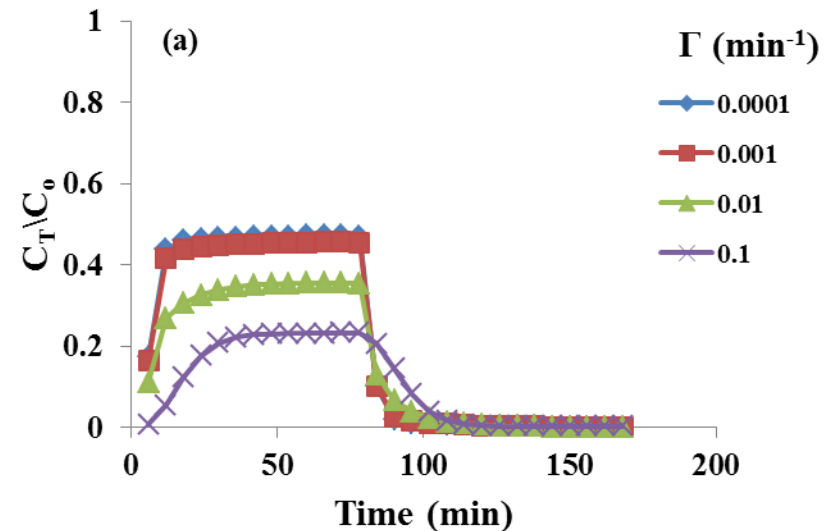
SSTM – Single Permeability Per Tube

- Example of pathogen transport
- Pathogens are quickly removed from low velocity regions.
- Pathogen transport continues for greater distances in high velocity regions.
- This produces hyper-exponential retention profiles, especially for greater retention rates and large velocity distributions.



SSTM – Dual Permeability Per Tube

- Example of pathogen transport
- Greater exchange produces less transport and lower variance in concentration.
- SSTM with single permeability per tube provides a worst case pathogen transport scenario, but is may be too conservative.



Conclusions

- The setback distance increases with velocity.
- High velocity regions will control the risk of infection.
- Stream tube models have several advantages over deterministic approaches (PDFs instead of explicit description of heterogeneity; mean and variance).
- Stream tube models may also account for mixing (dual permeability), hyper-exponential RPs, early breakthrough, and concentration tailing.
- SSTM with single permeability per tube provides a worst case transport scenario.